

Package ‘dppmix’

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Type Package

Title Determinantal Point Process Mixture Models

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Description Multivariate Gaussian mixture model with a determinant point process prior to promote the discovery of parsimonious components from observed data. See Xu, Mueller, Telesca (2016) <[doi:10.1111/biom.12482](https://doi.org/10.1111/biom.12482)>.

URL <https://bitbucket.org/djhshih/dppmix>

BugReports <https://bitbucket.org/djhshih/dppmix/issues>

Imports stats, mvtnorm

License GPL (>= 3)

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R topics documented:

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`dgammapois`*Density function for Gamma-Poisson distribution.*

Description

Data follow the Poisson distribution parameterized by a mean parameter that follows a gamma distribution.

Usage

```
dgammapois(x, a, b = 1, log = FALSE)
```

Arguments

| | |
|------------------|--|
| <code>x</code> | vector of x values |
| <code>a</code> | shape parameter for gamma distribution on mean parameter |
| <code>b</code> | rate parameter for gamma distribution on mean parameter |
| <code>log</code> | whether to return the density in log scale |

Value

density values

`dppmix_mvnorm`*Fit a determinantal point process multivariate normal mixture model.*

Description

Discover clusters in multidimensional data using a multivariate normal mixture model with a determinantal point process prior.

Usage

```
dppmix_mvnorm(  
  X,  
  hparams = NULL,  
  store = NULL,  
  control = NULL,  
  fixed = NULL,  
  verbose = TRUE  
)
```

Arguments

| | |
|----------------------|---|
| <code>X</code> | <code>N x J</code> data matrix of <code>N</code> observations and <code>J</code> features |
| <code>hparams</code> | a list of hyperparameter values: <code>delta</code> , <code>a0</code> , <code>b0</code> , <code>theta</code> , <code>sigma_prop_mu</code> |
| <code>store</code> | a vector of character strings specifying additional vars of interest; a value of <code>NA</code> indicates that samples of all parameters in the model will be stored |
| <code>control</code> | a list of control parameters: <code>niter</code> , <code>burnin</code> , <code>thin</code> |
| <code>fixed</code> | a list of fixed parameter values |
| <code>verbose</code> | whether to emit verbose message |

Details

A determinantal point process (DPP) prior is a repulsive prior. Compare to mixture models using independent priors, a DPP mixture model will often discover a parsimonious set of mixture components (clusters).

Model fitting is done by sampling parameters from the posterior distribution using a reversible jump Markov chain Monte Carlo sampling approach.

Given $X = [x_i]$, where each x_i is a D -dimensional real vector, we seek the posterior distribution the latent variable $z = [z_i]$, where each z_i is an integer representing cluster membership.

$$x_i | z_i \sim Normal(\mu_k, \Sigma_k)$$

$$z_i \sim Categorical(w)$$

$$w \sim Dirichlet([\delta \dots \delta])$$

$$\mu_k \sim DPP(C)$$

where C is the covariance function that evaluates the distances among the data points:

$$C(x_1, x_2) = \exp\left(-\sum_d \frac{(x_1 - x_2)^2}{\theta^2}\right)$$

We also define $\Sigma_k = E_k \Lambda_k E_k^T$, where E_k is an orthonormal matrix whose column represents eigenvectors. We further assume that $E_k = E$ is fixed across all cluster components so that E can be estimated as the eigenvectors of the covariance matrix of the data matrix X . Finally, we put a prior on the entries of the Λ_k diagonal matrix:

$$\lambda_{kd}^{-1} \sim Gamma(a_0, b_0)$$

Hence, the hyperparameters of the model include: `delta`, `a0`, `b0`, `theta`, as well as sampling hyperparameter `sigma_pro_mu`, which controls the spread of the Gaussian proposal distribution for the random-walk Metropolis-Hastings update of the μ parameter.

The parameters (and their dimensions) in the model include: K , z ($N \times 1$), w ($K \times 1$), λ ($K \times J$), μ ($K \times J$), Σ ($J \times J \times K$). If any parameter is fixed, then K must be fixed as well.

Value

a dppmix_mcmc object containing posterior samples of the parameters

References

Yanxun Xu, Peter Mueller, Donatello Telesca. Bayesian Inference for Latent Biologic Structure with Determinantal Point Processes. *Biometrics*. 2016;72(3):955-64.

Examples

```
set.seed(1)
ns <- c(3, 3)
means <- list(c(-6, -3), c(0, 4))
d <- rmvnorm_clusters(ns, means)

mcmc <- dppmix_mvnorm(d$X, verbose=FALSE)
res <- estimate(mcmc)
table(d$c1, res$z)
```

estimate

Estimate parameter.

Description

Estimate parameter from fitted model.

Usage

```
estimate(object, pars, ...)
```

Arguments

| | |
|--------|---------------------------------|
| object | fitted model |
| pars | names of parameters to estimate |
| ... | other parameters to pass |

| | |
|-------|---|
| rbern | <i>Random generator for the Bernoulli distribution.</i> |
|-------|---|

Description

Random generator for the Bernoulli distribution.

Usage

```
rbern(n, prob)
```

Arguments

| | |
|------|-------------------------------|
| n | number of samples to generate |
| prob | event probability |

Value

an integer vector of 0 (non-event) and 1 (event)

| | |
|-------|---|
| rbvec | <i>Generate a random binary vector.</i> |
|-------|---|

Description

Generate a random binary vector.

Usage

```
rbvec(n, prob, e.min = 0)
```

Arguments

| | |
|-------|---|
| n | size of binary vector |
| prob | event probability (not accounting for minimum event constraint) |
| e.min | minimum number of events |

Value

an integer vector of 0 and 1

| | |
|------------|---|
| rdirichlet | <i>Random generator for the Dirichlet distribution.</i> |
|------------|---|

Description

Random generator for the Dirichlet distribution.

Usage

```
rdirichlet(n, alpha)
```

Arguments

| | |
|-------|--|
| n | number of vectors to generate |
| alpha | vector of parameters of the Dirichlet distribution |

Value

a matrix in which each row vector is Dirichlet distributed

| | |
|------------------|--|
| rmvnorm_clusters | <i>Generate random multivariate clusters</i> |
|------------------|--|

Description

Generate random multivariate clusters

Usage

```
rmvnorm_clusters(ns, means)
```

Arguments

| | |
|-------|---------------------------------------|
| ns | number of data points in each cluster |
| means | centers of each cluster |

Value

list containing matrix X and labels cl

Examples

```
ns <- c(5, 8, 7)
means <- list(c(-6, 1), c(-1, -1), c(0, 4))
d <- rmvnorm_clusters(ns, means)
```

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